Prediction of structural forces of segmental tunnel lining using FEM based artificial neural network

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ABSTRACT

Article History: Received 29 December 2016, Revised 11 January 2017, Accepted 14 January 2017.

The critical parameters in investigating the performance of designed support system of tunnels are the structural forces i.e. peak values of axial and shear forces, and moments. In this research, a complete database was firstly prepared using finite element method. Using finite element models, we modeled the segmental tunnel lining that was composed of 5+1 concrete segments in one ring. Then, an artificial neural network (ANN) model of multi-layer perceptron was developed to estimate the lining structural forces. To do this, the number of neurons and their arrangement were optimized based on the obtained minimum values from the root mean square error (RMSE). To prove the efficiency of the developed ANN model, we calculated the coefficient of efficiency (CE), determination coefficient (R²), variance account for (VAF), and RMSE values. The results demonstrated a promising precision and high efficiency of the presented ANN method for estimating the structural forces of tunnel lining composed of concrete segments instead of alternative costly and tedious solutions. Finally, the sensitivity analysis showed that among the input variables, the tunnel cover is the most influencing variable on the lining structural forces. However, other input variables, i.e. lateral earth pressure and key segment position were the second important variables affecting the induced stresses on tunnel lining.

Keywords : Artificial neural network, Lining, Multi-layer perceptron, Segment, Tunnel

1. Introduction

Support system of tunnels that are excavated by shield TBMs (Tunnel Boring Machine) is generally composed of segments with reinforced concrete (RC). Assembling these concrete segments inside the tunnel excavation shield forms the tunnel support rings. Construction of RC segments is a crucial step in tunnel construction procedure [1-4]. Due to the simplicity in installation and the assembling operation of a ring, one segment has to be designed smaller than the others which is called the key segment that is installed at the end of the ring. Fig 1 shows the assembled ring of RC segments in segment manufacturing factory [5]. Design methods of RC segments can be classified in three approaches: laboratory or experimental methods, closed form solutions or analytical

methods, and numerical methods, closed form solutions of analytical methods. Analytical solutions have been extended from the beginning of underground openings designing until now [1, 6-16]. Some analytical solutions are restricted either to only elastic behavior of materials or

only to shallow tunnels. Some others, taking into consideration few simple assumptions with reduced stiffness of segmental support ring with respect to the continuous ring without longitudinal joints and do not consider key segment shape and size in comparison with other segments in the assembled ring.

Recently, some design and monitoring processes of RC segmental tunnel lining behaviour were done through laboratorial experiments [6; 21; 22; 26; 29; 30; 32]. The experimental approaches are very reliable methods than analytical and numerical methods, but these methods are often expensive and tedious.

To overcome the experimental and analytical defects, numerical solutions have been extended widely in last decades [1; 2; 3; 7; 9; 13].

However, the numerical solutions are often time-consuming and need more detailed data that could be unidentified during analysis. The output results of numerical attempts should be verified by either experimental or analytical solutions or by in-field monitoring results. In last years, innovative methods like Artificial Neural Network (ANN) have been applied as a prediction tool to study the complex problems. Such approaches have been extended widely in geotechnical and geomechanical engineering problems [4; 5; 12; 14; 16; 17; 18; 19; 20; 23; 27; 28; 31]. As the above mentioned defects of the triple individual approaches reveal, ANN methods seem to be new alternative solutions. Estimation of structural forces in RC segments of tunnel lining structure using ANN has not been studied in detail as of yet. In this paper, ANN method was applied to estimate the structural forces of RC segments in tunnel lining structure based on the results of finite element method. Sensitivity analysis of variables was performed to assess their influence on the output results. Finally the applicability and efficiency of the designed ANN model were evaluated using RMSE (%), R², VAF (%), and CE indices.

2. The Concept of artificial neural network

Artificial neural networks are consisted of many data processing units called neurons. By using neurons, the network are capable to simulate the operation of human brain nature on the basis of trial and error method [34, 43]. In a common ANN model, there is a huge number of interconnections among the neurons. Generally, an ANN model is mostly composed of three layers named: input layer, hidden layer(s) and output layer. Schematic view of a usual ANN is illustrated in Fig. 2.

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(2)



Fig. 1. Assembled ring from RC segments in segment manufacturing factory, Tehran metro project, Line 4

Hidden layer(s) is the important layer of one neural network model because the main calculation phase is performed in it. Neurons in each layer are linked to the neurons of nearby layer with a coefficient named weight (w). Outputs of input layer is as input signal for the hidden layer(s) and the similar rule is governed between hidden layer(s) and output layer, respectively. Optimized number of neurons and hidden layers are calculated based on the trial and error rule and the goal error value [34].



Fig. 2. An illustration of a usual ANN [10]

ANN is trained at first and consequently tested and verified by other different data. In training process, inputs are entered and outputs values are determined. Then the error between the real and predicted values is calculated. Base on calculated error value, the weights are adjusted by starting from the last output layer towards the first input layer; this procedure is known as back propagation algorithm. Back propagation algorithms are potent implements for models with prediction aims [10]. Perceptron Neural network model was proposed by Rosenblatt [24]. Multi-layer perceptron NN, on the other hand, was improved and proposed by Rumelhart [25]. In this model, the input layer normalizes the input values. This type of data preparation and normalization improves the network performances, because of more homogeneous scattering of normalized data, as illustrated in Fig 3. This method of data normalization has been utilized by many researches [11; 15; 28]. Multilayer perceptron (MLP) is an adjustment of the linear standard perceptron which can separate data without capability of linearly separation [8].



Fig. 3. Homogeneous distribution of data after normalization process [11].

3. Database

3.1. Numerical analysis

Application of NN model of multi-layer perceptron for estimation of structural forces of RC segments in tunnel lining, requires to supply a comprehensive database. To do this, we used the resulted values from finite element (FE) analysis (ABAQUS 2014, Version 6.14. Abaqus, Inc., Pawtucket, Providence, R.I.). In the designed numerical model of tunnel lining, the support structure in one ring consisted of 5+1 segments. The engineering and geometrical characteristics of RC segments are summarized in Table 1. From size point of view, in one ring, five RC segments (A2-A6) were almost similar to each other. To decrease the total calculation time of numerical modelling, soil elements are neglected in the FE model. Therefore, the beam-spring method was applied to model the structure of tunnel lining [1, 2]. In this method the effects of soil body on the exterior side of tunnel lining and interaction between them were simulated using tangential and radial springs. Because of their negligible effects with respect to radial springs, tangential springs were neglected. Stiffness of soil radial springs is calculated using the following Eq. (1) [49]:

$$K = \frac{A.E}{R.(1+\nu)}$$
(1)
Where, K is stiffness of radial spring, E is Young modulus of soil, v is

Where, *K* is stiffness of radial spring, *E* is Young modulus of soil, *v* is poison's ratio of soil, *R* is tunnel radius, and *A* is effective area on the exterior side of lining structure that is subjected to applied load because of the soil, and calculated by Eq. (2):

$$A = R\theta b \tag{2}$$

Where, θ is the angle in terms of radial between 2 successive radial springs, and b is effective area of each spring in tunnel longitudinal direction. Figs. 4(a)-(b) show the perspective and non-perspective views of an assembled ring under soil radial springs. In structural modelling, load from surrounding ground was applied radially towards tunnel lining, Fig. 5. Normal radial stresses applied on tunnel lining structure are calculated by Eq. (3):

$$\sigma_{\mu 0} = \sigma_{\mu 0} \cos^2 \theta + \sigma_{\mu 0} \sin^2 \theta \tag{5}$$

Where, σ_{n0} is the normal stress, σ_{v0} is the vertical stress, σ_{h0} is the horizontal stress, and θ is radial angle measured from tunnel bottom [1].



(a) Non-perspective view







Fig. 5. Applied radial load from the surrounding ground on tunnel lining exterior side

Table1.	Engineering and	geometrical	characteristics of	concrete segments
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		Enginee	Geometrical			
		Linghier	properties			
Segment No.	E(GPa)	v (poisson ratio)	ρ (kg/m ³)	Material behaviour	t (Thickness-cm)	Central angle (°)
A1(key				CDP		30
segment)	25	0.15	2350	(Concrete	30	50
A2-A6	-			damage		66
				plasticity)		

3D solid elements were used to model the segments of a ring. After assembling the concrete segments, the plane strain conditions were applied to the model. In current numerical models, it was assumed that the origin of angle in model plane is positioned at the tunnel crown (see Fig. 6(a)). Joints between two adjacent segments named longitudinal joints. Fig. 6(b) shows longitudinal joints of assembled segments in one individual ring and the position of key segment at θ =90°. The assembled ring is representative of support structure of tunnel lining. Hard contact was supposed for six concrete to concrete contact surfaces with frictional penalty coefficient of 0.4.

3.2. Data preparation

The model at first was solved for tunnel overburden H= 5m, K=0.47 (lateral earth pressure) and θ =0°. Then both H and K parameters were

kept constant and θ value changed to 30°, 60°, 90°, 120°, 150° and 180°, respectively. This sort of variation for input parameters, was considered for H=15 m, 25m and K=0.47 and 1.0 (Hydrostatic condition of the ground). Straight type of longitudinal joints, i.e. parallel with z-axis were considered. Key segment positions at 210°, 240°, 270°, 300° and 330° were neglected because of the axisymmetric geometry of assembled ring. Tunnel lining under the ground load is shown in Fig. 7. Finally, 42 data sets were obtained. Input data variables and resulted output are presented in Table 2. Fig 8 shows the output values resulted for shear and axial force and moment quantities for an arbitrary section of the modelled ring.



Fig.7. Tunnel lining structure underground radial load





Fig. 8. Resulted axial force (N) and shear force (N) and moment (N.M) for an arbitrary section of a segment in an assembled ring

3.3. Data normalization

To increase the processing and convergence rate of ANN during training process and to minimize the prediction error, raw data obtained from numerical models must be normalized [49].

Before commencing the modelling, all data must be filtered and the outliers should be deleted. Normalization of data proportionate all the variables with respect to each other. Traditionally, to normalize the data, the aforementioned approach means to fit the data within unity (1), herein all data values will be in the range of zero to unity. Unity-based normalization relation follows the Eq. 4 [50]:

$$u_{Norm} = \frac{u - u_{\min}}{u_{\max} - u_{\min}} \tag{4}$$

Where, u is any raw data, uNorm is the normalized data, umin is the minimum value of data and umax is the maximum value of data.

4. Design of optimum and model

The data obtained from FE models were applied to make the multi-layer perceptron model for prediction aim. In this study, all data were divided in 3 parts: training data (70% of total data), testing data (20% of total data) and validation data (10% of total data).

Optimized structure of NN model, i.e. arrangement of neurons in hidden layers and the number of hidden layers, should be calculated on the basis of trial and error rule.

At first, optimized number of neurons was calculated based on the obtained values of root mean square error (RMSE). To do this, different variety of neurons were embedded in hidden layers of the model and RMSE value was calculated according to Eq. 5:

$$RMSE = \sqrt{\frac{1}{N} \sum_{i=1}^{N} (\hat{u}_{k} - u_{k})^{2}}$$
(5)

Where, \hat{u}_k and \hat{u}_k are the kth predicted and observed values of target, respectively, and N is the number of observations for which the error has been computed.

The results are illustrated in Fig. 9. It can be concluded that the minimum value of RMSE was obtained by 6 number of neurons. Thereafter, these neurons must be arranged in one or two hidden layers.

Flood et al. [47] stated that MLP model with two minimum hidden layers provides more flexibility for modelling complex problems.

Table 2. Raw data resulted from the finite element method

nput variables				Output parameters						
No	к	Height (m)	θ (°)	М _{ши} (N.m)*	M _{min} (N.m)*	$\tau_{max} (N)^{**}$	τ _{min} (N)**	F _{max} (N)***	F _{min} (N)***	
1	0.4	5	0	2788	-	18060	-	43660	35000	
2	074	5	30	28366	3203	14 0 90	20600	43080	35 0 40	
3	074	5	60	29026	31645	20050	17040	43060	35 2 00	
4	074	5	90	28945	30972	19 9 90	15620	44 0 20	35 0 30	
5	074	5	12	2875	30225	18 8 90	21050	44 0 10	35080	
6	074	5	13	27084	29917	13 6 20	15 8 50	43040	34 0 70	
7	074	5	138	30031	30660	80 9 90	23 0 70	44020	35 2 20	
8	ĩ	5	0	6559	33001	4408	24090	67 8 40	46 0 20	
9	1	5	30	71386	6 537 9	4 60 8	54 0 00	67 8 20	47040	
10	1	5	60	63386	58949	350050	35 6 70	65 0 10	45 6 90	
11	1	5	90	70048	64663	46 9 90	50 6 10	67 0 60	45 9 70	
12	1	5	12	65020	6265	35 0 30	49 0 10	66 9 30	45 6 70	
13	1	5	13	6833	6682	42770	52 0 50	67070	47 0 20	
14	1	5	128	66003	60663	4694060	28 6 40	67050	46 0 50	
15	0.4	15	0	15044	62986	86 0 10	16 8 80	13090	85 0 40	
16	074	15	30	1002	14631	860240	10 6 00	1404630	89 0 30	
17	074	15	60	1028	1 60 0	10200	110000	1404090	87070	
18	074	15	90	1003	1 48 8	100090	86670	150080	89070	
19	074	15	12	1498	10001	103650	91 9 30	155630	86 9 60	
20	074	15	v	1007	16404	110260	69 0 90	133020	91030	
21	074	15	128	1 00 3	10109	10810	86 9 40	133360	87 6 70	
22	T	15	0	7007	1 66 6	4403030	10 8 70	169910	15070	
23	1	15	30	7065	6 9 06	4602	5004050	16810	150680	
24	1	15	60	69944	6638	325000	38 0 70	163090	152010	
25	1	15	90	68993	6 75 1	40610	53 0 00	1638640	151650	
26	1	15	12	6965	7 1£7 7	42030	55 6 00	163380	150060	
27	1	15	ъ	67069	70£29	43060	54 0 10	163070	15000	
28	1	15	128	71047	70011	50@10	28920	163330	15030	
29	0.4	25	0	17010	67000	10 0 70	14 6 80	1706040	9 789 0	
30	074	25	30	1062	18830	7207030	12010	110404-0	75 9 50	
31	074	25	60	1000	1008	93 0 10	9204030	1208060	79 6 00	
32	074	25	90	1 68 0	1665	12010	81040	189070	10 9 10	
33	074	25	12	1 00 7	1860	759000	13040	12000	7433880	
34	074	25	ß	1 60 5	1003	13 0 00	850090	1703640	10 @ 20	
35	074	25	138	1009	1 99 9	1228330	99 6 90	1706040	988680	
36	T	25	0	70109	1802	4404010	10030	250010	23 0 30	
37	1	25	30	69099	7 00 0	45 0 30	5303060	249000	23250	
38	1	25	60	68869	69918	31 6 20	40020	249990	230040	
39	1	25	90	68038	70 B 6	40042	55 8 70	249920	230020	
40	1	25	12	68018	74668	4 60 0	58 6 80	249980	230070	
41	1	25	ıs	6 7 83	7 3 86	4 00 9	57090	249950	230050	
42	1	25	128	70045	7 3 915	5301040	28 9 10	24 9 20	230040	
			0	0	7006	0	14020	00	00	

Then, different arrangement of 6 neurons were considered in two hidden layers. Based on two activation functions, i.e. TANSIG and LOGSIG (tangential and logarithmic nonlinear sigmoid transform functions generally used in ANN), the resulted RMSE values are presented in Table 3.

N



Fig. 9. Optimum number of neurons in hidden layer(s) based on minimum value for RMSE

It can be concluded that model has the best efficiency in 3-4-2-1 for neurons arrangement based on the minimum RMSE value. Finally, schematic architecture of optimized network is shown in Fig. 10.

Table 3. Optimum arrangement of neurons in hidden layers

	Network	RMSE	RMSE	
No.	arrangement	(Transfer Function:	(Transfer Function:	
	arrangement	TANSIG)	LOGSIG)	
1	3-6-1	0.04	0.10	
2	3-1-5-1	0.51	0.11	
3	3-2-4-1	0.07	0.08	
4	3-3-3-1	0.02	0.04	
5	3-4-2-1	0.01	0.01	
6	3-5-1-1	0.05	0.03	



Fig. 10. Architecture of Optimized MLP neural network

5. Results and discussion

5.1. Model performance evaluation

Performance of artificial neural network should be assessed in predicting the capability of outputs. Therefore, four performance indices including determination coefficient (R2), variance account for (VAF), coefficient of efficiency (CE) and root mean square error (RMSE) were selected and calculated using testing data sets. These data sets were selected randomly from the database and were not included in training phase. VAF and CE values were calculated from Eqs. (6)–(7):

$$VAF = 100 \times \left(1 - \frac{\operatorname{var}(u_k - \hat{u}_k)}{\operatorname{var}(u_k)}\right)$$
(6)

$$CE = 1 - \frac{\sum_{k=1}^{N} (\hat{u}_k - u_k)^2}{\sum_{k=1}^{N} (\hat{u}_k - \overline{\hat{u}}_k)^2}$$
(7)

Where, var represents the variance, and are the kth measured and predicted values respectively, is the mean of predicted values, and N is the number of data sets. The VAF index express the intensity of variances discrepancy between the measured and predicted datasets. The values of VAF close to 100 % mean low inconsistencies, and therefore, better prediction capabilities. The lower RMSE, the better network's performance [51, 52]. In an ideal condition, the RMSE value must be zero and the CE value must be 1.0. The graphs of R2 for output parameters are shown in Figs. 11(a)-(f).Table 4 presents the obtained values of performance indices.



1









Table 4. Performance indices of the model

Perform	Output parameters								
Index	M(Mome nt) _{max}	M(Mome nt) _{min}	τ(Shea r) _{max}	τ(Shea r) _{min}	F(Axia l) _{max}	F(Axia 1) _{min}			
RMSE (%)	7	8	12	11	9	5			
R ²	0.962	0.95	0.92	0.95	0.84	0.98			
VAF (%)	94.21	94.36	91.54	89.3	88.9	98.4			
CE	0.91	0.94	0.89	0.89	0.81	0.98			

5.2. Sensitivity analysis

To determine the effect of each input parameter on output values, sensitivity analysis was performed. A useful method is cosine amplitude method (CAM) [53]. Data components form a data vector, X, are defined as:

$X = \{x_1, x_2, x_3, \dots, x_n\}$

Every component xi in the data vector X, is a vector with m dimension, i.e.,

$$\mathbf{x}_{i} = \{\mathbf{x}_{i1}, \mathbf{x}_{i2}, \mathbf{x}_{i3}, \dots, \mathbf{x}_{im}\}$$

Hence, all data can be assumed as a point in m-dimensional space, where each point has m coordinates for a full description. Each element of a relation, rij, results from a mutual comparison of two data pairs, i.e. xi and xj. The strength of the relationship between vector xi and vector xj is defined by Eq. (6):

$$i_{jj} = \frac{\left|\sum_{k=1}^{m} x_{ik} x_{jk}\right|}{\sqrt{\left(\sum_{k=1}^{m} x_{ik}^{2}\right)\left(\sum_{k=1}^{m} x_{jk}^{2}\right)}}$$
(6)

Where, rij is strength of relations between input and output parameters, and i, j =1, 2, ..., n. Eq. (6) defines that this method is the dot product of the cosine function. When two vectors are collinear (most similar), dot product will be unity; when orientation of 2 vectors have 90° of angle with respect to each other (most dissimilar), dot product will be zero. Figs. 12(a)-(f) show the strength values of relations (rij) between input (H, K, θ) and output parameters.

As can be seen from the Figs. 11(a)-(f), the overburden of buried tunnel or Height (H) input variable is the most efficient parameter on the resulted outputs than the other parameters two, and K value (lateral earth pressure) has the least influence on outputs except for Mmin and Fmin outputs.













Fig. 12. Strength of relation (r_{ij}) between input and output parameters

6. Conclusion

The peak values of structural forces were determined for the structure of segmental tunnel lining ring using the ANN method. Neural network model of multi-layer perceptron was applied. At first, based on the minimum obtained values of RMSE from the input data variables, the number of neurons and their arrangement in hidden layers were determined and optimized. It was concluded that in 3-4-2-1 arrangement of neurons in the network, the resulted value of RMSE was 0.01 both for LOGSIG and TANSIG transfer functions. Then the NN model was tested and validated using different data. The efficiency of presented NN model was evaluated using the RMSE, R2, VAF and CE indices. The obtained results presented the high capability of the NN model in prediction and estimation of structural forces in segmental lining of tunnel, and this prediction method can be employed to gain reliable results for primary design of segmental tunnel lining instead of current tedious and expensive methods.

Finally, the sensitivity analyses were conducted to evaluate the effect of each input variable on the output parameters. It was found that the tunnel height or overburden parameter (H), among other input variables, had the highest influence on outputs, and the K parameter (lateral earth pressure) had the least effect on outputs. The reason is that the tunnel height is the main source of induced stresses on tunnel lining. On the other hand, other input variables, i.e. the lateral earth pressure and key segment position had the second order of importance on induced stresses than the tunnel height value.

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